## LOYOLA COLLEGE (AUTONOMOUS), CHENNAI - 600034

## B.Sc. DEGREE EXAMINATION - STATISTICS <br> FIFTH SEMESTER - NOVEMBER 2013 <br> ST 5507/5503-COMPUTATIONAL STATISTICS

Date : 12/11/2013
Dept. No. $\square$ Max. : 100 Marks
Time : 9:00-12:00

Answer any THREE of the following:

1) a) Calculate seasonal indices by the ratio-to-moving average method from the following data:

| QUARTER | YEAR |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 2001 | 2002 | 2003 | 2004 |
| $\mathrm{Q}_{1}$ | 75 | 86 | 90 | 100 |
| $\mathrm{Q}_{2}$ | 60 | 65 | 72 | 78 |
| $\mathrm{Q}_{3}$ | 54 | 63 | 66 | 72 |
| $\mathrm{Q}_{4}$ | 59 | 80 | 85 | 93 |

b) Fit a straight line trend by the method of least squares to the following data relating to the sales of a leading departmental store.

| Year | 1997 | 1998 | 1999 | 2000 | 2001 | 2002 | 2003 | 2004 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Sales <br> (Rs. In crores) | 76 | 80 | 130 | 144 | 138 | 120 | 174 | 190 |

c) From the following data find Laspeyre's, Paasche's and Fisher's price and quantity index numbers.

|  | 1995 |  | 2005 |  |
| :---: | :---: | :---: | :---: | :---: |
| Commodities | Price | Quantity | Price | Quantity |
| A | 20 | 8 | 40 | 6 |
| B | 50 | 10 | 60 | 5 |
| C | 40 | 15 | 50 | 15 |
| D | 20 | 20 | 20 | 25 |

2) a) The mean height of 50 male students who showed above average participation in college athletics was 68.2 inches with a standard deviation of 2.5 inches, while 50 male students who showed no interest in such participation had a mean height of 67.5 inches with a standard deviation of 2.8 inches. Test the hypothesis that male students who participated in college athletics are taller than other male students. Use 5\% significance level.
b) A random sample of 10 boys had the following IQ's 72, 122, 112, 103, 90, 85, 97, 100, 109 and 102. Do these data support the assumption of a population mean IQ of 105 ? Use $1 \%$ level of significance.
c) The following data give frequency of aircraft accidents experienced by 2546 pilots during a four year period:

| No. of accidents | 0 | 1 | 2 | 3 | 4 | 5 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 2036 | 422 | 71 | 13 | 3 | 1 |

Fit a Poisson distribution and test the goodness of fit at $5 \%$ level of significance. $\quad(8+10+15)$
3) The following table represents the summary of data for complete census of all the 2010 farms in a region. The farms were stratified according to farm-size in acres into seven strata, as shown in the table.

| Stratum No. | Farm size <br> (in acres) | No. of Farms <br> $\left(\mathrm{N}_{\mathrm{i}}\right)$ | Averyme area <br> under wimeat per <br> farmacres. <br> $(\bar{T}$ <br> $\left.\bar{l}_{i}\right)$ | Standard <br> deviations of <br> area under Wheat <br> per farm in acres <br> $\mathrm{S}_{\mathrm{i}}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | $0-40$ | 394 | 5.4 | 8.3 |
| 2 | $41-80$ | 461 | 16.3 | 13.3 |
| 3 | $81-120$ | 391 | 24.3 | 15.1 |
| 4 | $121-160$ | 334 | 34.5 | 19.8 |
| 5 | $161-200$ | 169 | 42.1 | 24.5 |
| 6 | $201-240$ | 113 | 50.1 | 26.0 |
| 7 | More than 240 | 148 | 63.8 | 35.2 |

Calculate the sampling variance of the estimates area under wheat for the region from a sample of 150 farms: (i) if the farms are selected by the method of srs without stratification and (ii) if the farms are selected by the method of srs within each stratum and allocated in proportion to (a) the number of farms in each stratum $\mathrm{N}_{\mathrm{i}}$, and (b) the product $\mathrm{N}_{\mathrm{i}} \mathrm{S}_{\mathrm{i}}$.
4) a. Twelve 3 -year-old boys and ten 3 -year-old girls were observed during two sessions of recess in a nursery school. Each child's play was scored for incidence and degree of aggression as follows:

| Boys: 96 | 65 | 74 | 78 | 82 | 121 | 68 | 79 | 111 | 48 | 53 | 92 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Girls: | 12 | 47 | 32 | 59 | 83 | 14 | 32 | 15 | 17 | 82 |  |

At $5 \%$ level, is there evidence to suggest that there are gender differences in the incidence and amount of aggression? Use Wald-Wolfowitz Run test.
b. Random sample of two models of scooters were tested for mileage.

| BAJAJ | $:$ | 60 | 54 | 76 | 48 | 66 | 52 | 62 | 72 | 68 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| HONDA | $:$ | 62 | 58 | 52 | 48 | 70 | 56 | 47 | 70 |  |

Use Mann-whitney U- test, at 5\% level of significance, test whether the average mileage of these two models are same.
5) a) 500 apples are taken at random from a large basket and 50 are found to be bad. Estimate the proportion of bad apples in the basket and assign limits within which the percentage most probably lies.
b) Salt free diets are often prescribed to people with high blood pressure. The following data were obtained from an experiment designed to estimate the reduction in diastolic blood pressure as a result of following a salt - free diet for two weeks. Assume the diastolic readings are normally distributed.

| Before | 93 | 106 | 87 | 92 | 102 | 95 | 88 | 110 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| After | 92 | 102 | 89 | 92 | 101 | 96 | 88 | 105 |

To determine whether Salt free diets had any effect on reduction in diastolic blood pressure.
c) A man buys 50 electric bulbs of Phillips and 50 electric bulbs of Crompton. He finds that Phillips bulbs give an average life of 1500 hours with standard deviation of 60 hours and Crompton bulbs give an average life of 1512 hours with a standard deviation of 80 hours. Is there a significant difference in the mean life of the two makes of bulbs?

